

1) If $f(x, y) = 2x + 3x^2y$ find the following:

a) $\int_0^3 f(x, y) dx$

b) $\int_0^4 f(x, y) dy$

2) Calculate the following iterated integrals:

a) $\int_1^3 \int_0^1 (1 + 4xy) dx dy$

b) $\int_0^2 \int_0^{\pi/2} x \sin y dy dx$

c) $\int_0^1 \int_1^2 \frac{xe^x}{y} dy dx$

d) $\int_0^{\ln 2} \int_0^{\ln 5} e^{2x-y} dx dy$

3) Calculate the following double integrals:

a) $\iint_R (6x^2y^3 - 5y^4) dA, \quad R = \{(x, y) \mid 0 \leq x \leq 3, 0 \leq y \leq 1\}$

b) $\iint_R \frac{xy^2}{x^2 + 1} dA, \quad R = \{(x, y) \mid 0 \leq x \leq 1, -3 \leq y \leq 3\}$

c) $\iint_R \frac{x}{1 + xy} dA, \quad R = [0, 1] \times [0, 1]$

- 4) Sketch the solid whose volume is given by the iterated integral $\int_0^1 \int_0^1 (2 - x^2 - y^2) dy dx$.
- 5) Find the volume of the solid that lies under the hyperbolic paraboloid $z = 4 + x^2 - y^2$ and above the square $R = [-1, 1] \times [0, 2]$.
- 6) Find the volume of the solid bounded by the elliptic paraboloid $z = 1 + (x - 1)^2 + 4y^2$, the planes $x = 3$ and $y = 2$, and the coordinate planes.